

Soft Pattern Matching: Toward Runtime Verification of NLP Systems

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Based on H. Deguchi, G. Kamoda, Y. Matsushita, C. Taguchi, K. Suenaga, M. Waga, and S. Yokoi "A Soft and Fast Pattern Matcher for Billion-Scale Corpus Searches." ICLR 2025

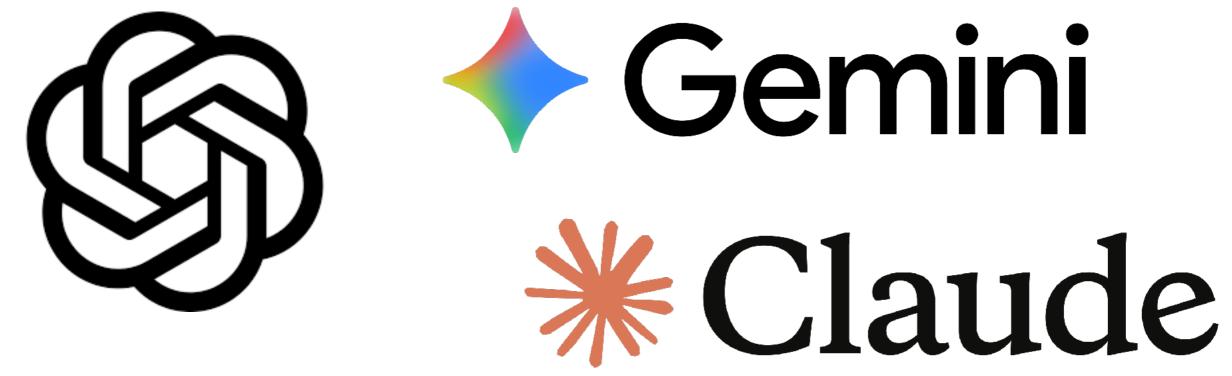
Personal Scientific Background

- Mainly working on CPS verification
- White-box system model is unnecessary!
- · Particularly, runtime verification, e.g., monitoring & testing
- Some Keywords:
 - Signal Temporal Logic

w/ quantitative semantics based on distance

- Extension of LTL for continuous signals
- (Timed) Pattern Matching
 - Extract relevant parts of log wrt. formal spec.

LLM Era

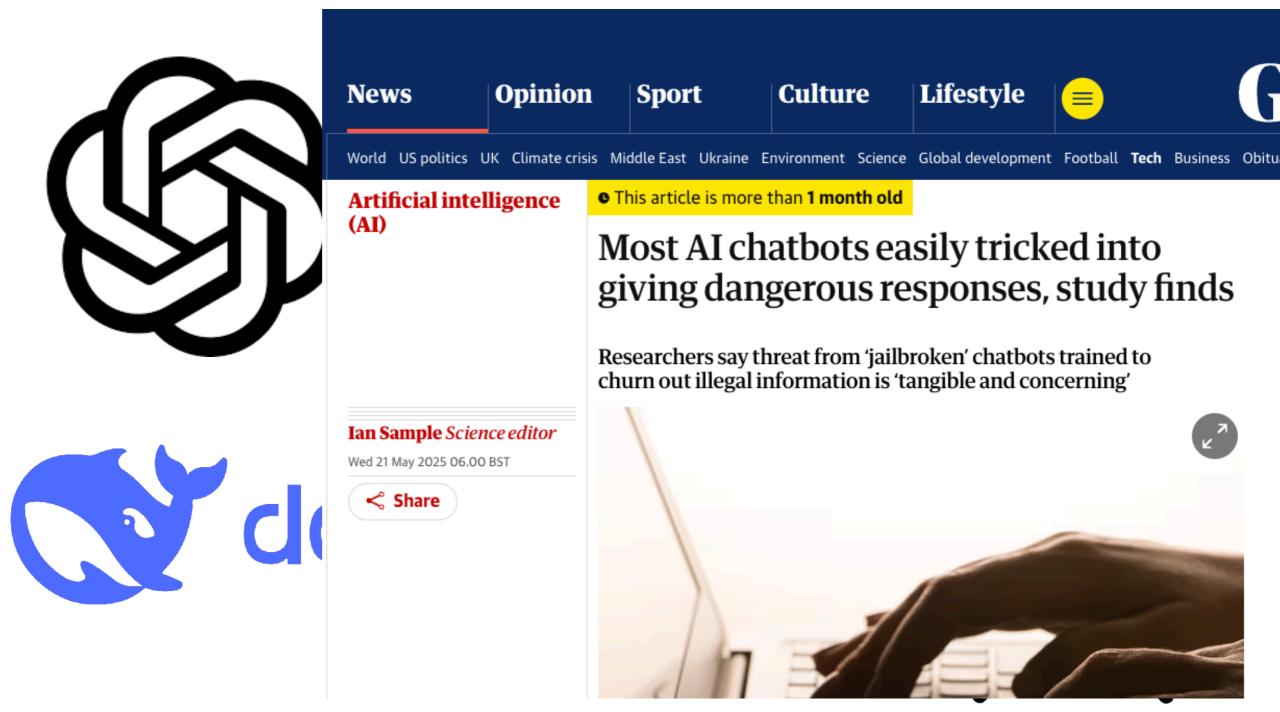






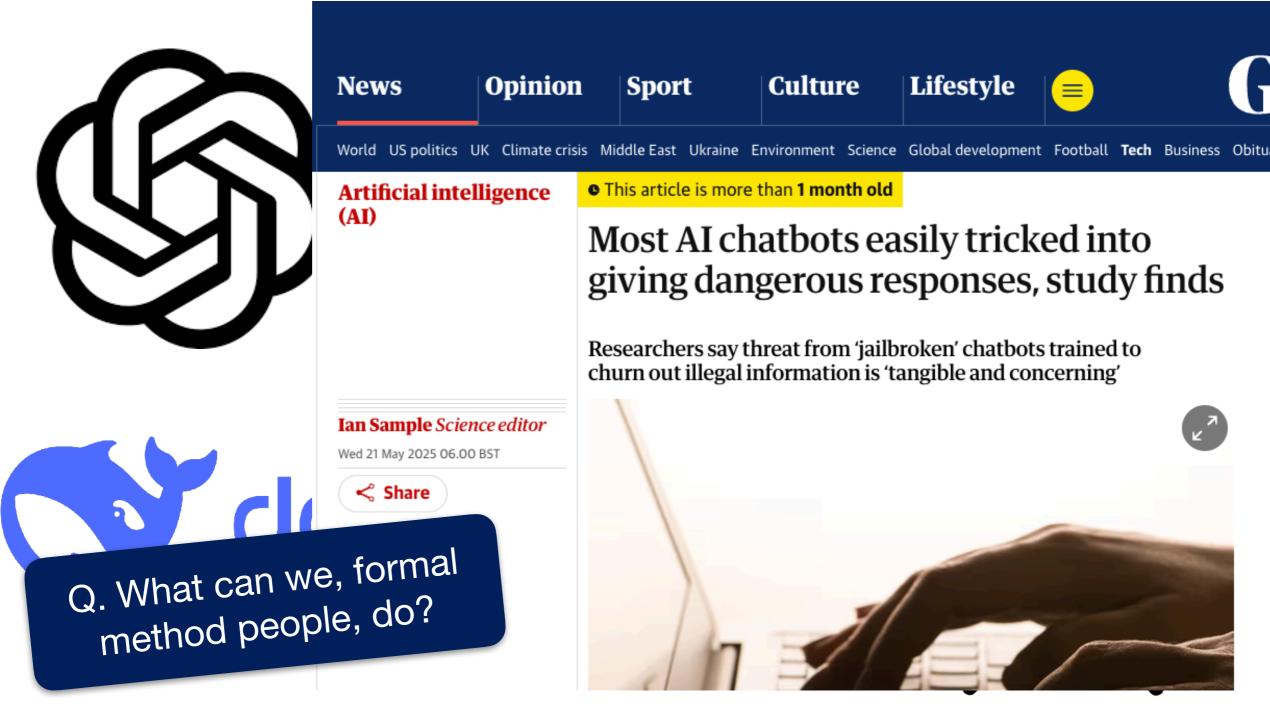
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Observations on LLM

System is extremely huge

Similar in CPS verification

- Fully exhaustive verification is likely impossible
- Inputs and outputs are mainly natural language texts
 - Writing spec. w/ conventional logics seems hard
 - Similarity of words should be included in the semantics
 - e.g. "My son is big" $\models \varphi \iff$ "My son is large" $\models \varphi$

Continuous-time version of LTL + distance from threshold

$$\varphi ::= \mu > 0 \mid \varphi \wedge \varphi \mid \neg \varphi \mid \varphi \mathcal{U}_I \varphi$$

Distance from the threshold

Qualitative (Boolean) Semantics

$$\begin{split} \sigma, t \models \mu > 0 &\iff \mu(\sigma(t)) > 0 \\ \sigma, t \models \varphi_1 \land \varphi_2 \\ &\iff \sigma, t \models \varphi_1 \text{ and } \sigma, t \models \varphi_2 \\ \sigma, t \models \neg \varphi &\iff \sigma, t \not\models \varphi \\ \vdots \end{split}$$

$$\begin{split} \rho(\sigma,t,\mu>0) &= \mu(\sigma(t)) \\ \rho(\sigma,t,\varphi_1 \wedge \varphi_2) \\ &= \min\{\rho(\sigma,t,\varphi_1),\rho(\sigma,t,\varphi_2)\} \\ \rho(\sigma,t,\neg\varphi) &= -\rho(\sigma,t,\varphi) \\ \vdots \end{split}$$

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$$\vdots$$

$$\rho(\sigma, t, \mu > 0) = \mu(\sigma(t))$$

$$\rho(\sigma, t, \varphi_1 \land \varphi_2)$$

$$= \min\{\rho(\sigma, t, \varphi_1), \rho(\sigma, t, \varphi_2)\}$$

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Continuous-time version of LTL + distance from threshold

$$\varphi ::= \left| \mu > 0 \right| |\varphi \wedge \varphi| |\neg \varphi| |\varphi \mathcal{U}_I \varphi$$

Distance from the threshold

Q. Good "distance" for natural languages?

Qualitative (Boolean) Semantics

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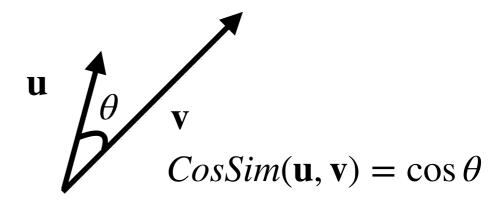
Our Choice: Word Embedding + Cosine Similarity

Word Embedding: Encode words as vectors

- $E \colon \text{Word} \to \mathbb{R}^N$
- Similar usage ≈ similar directions
 - e.g. "He is from Croatia" vs. "He is from Japan"

Cosine Similarity: Measure the similarity by directions

$$CosSim(\mathbf{u}, \mathbf{v}) = \frac{\mathbf{u} \cdot \mathbf{v}}{\|\mathbf{u}\| \|\mathbf{v}\|}$$



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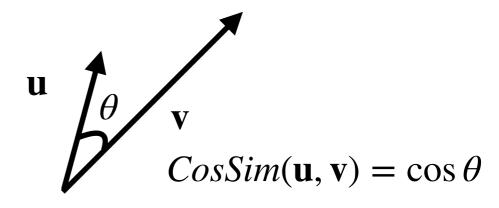
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Soft Pattern Matching

[Contribution]

String matching + pointwise comparison w/ CosSim and E

Inputs

Typically huge

- Target words: $w = w_1 w_2 ... w_n \in Word*$
- Pattern words: $p = p_1 p_2 ... p_m \in Word^*$
- Threshold: $\alpha \in \mathbb{R}$

Typically short

Output

Similarity is high for each word in pattern

• $Match_{\alpha}(w, p)$ s.t. $i \in Match_{\alpha}(w, p)$ iff. $\forall j \in \{1, ..., m\}$ $CosSim(E(w_{i+j-1}), E(p_j)) > \alpha$

Example of Soft Pattern Matching

Inputs

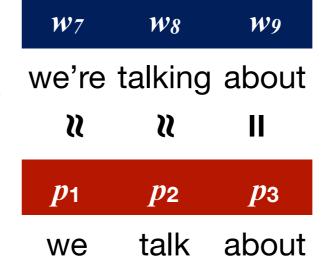
Target w

	W1	w_2	w ₃	W4	W5	<i>W</i> 6	<i>W</i> 7	w8	W9	W10	W11	W12	W13	W14
-	we	talk	like	we	know	what	we're	talking	about	when	we	talk	about	love

• Pattern: p p_1 p_2 p_3 we talk about

<u>Output</u>

• $Match_{\alpha}(w,p) = \{7,11\}$



W11	W12	<i>W</i> 13
we	talk	about
П	Ш	II
<i>p</i> 1	<i>p</i> 2	<i>p</i> 3
we	talk	about

Indexing-based Algorithm for Soft Pattern Matching

Offline indexing from target & Online operation on indices

Assumption: Many patterns for single (huge) target

Reasonable for, e.g. analysis of training data

Note: Algorithm for a stream of target is also available

Based on Quick Search for string matching

Step 0: Indexing from target

Target w

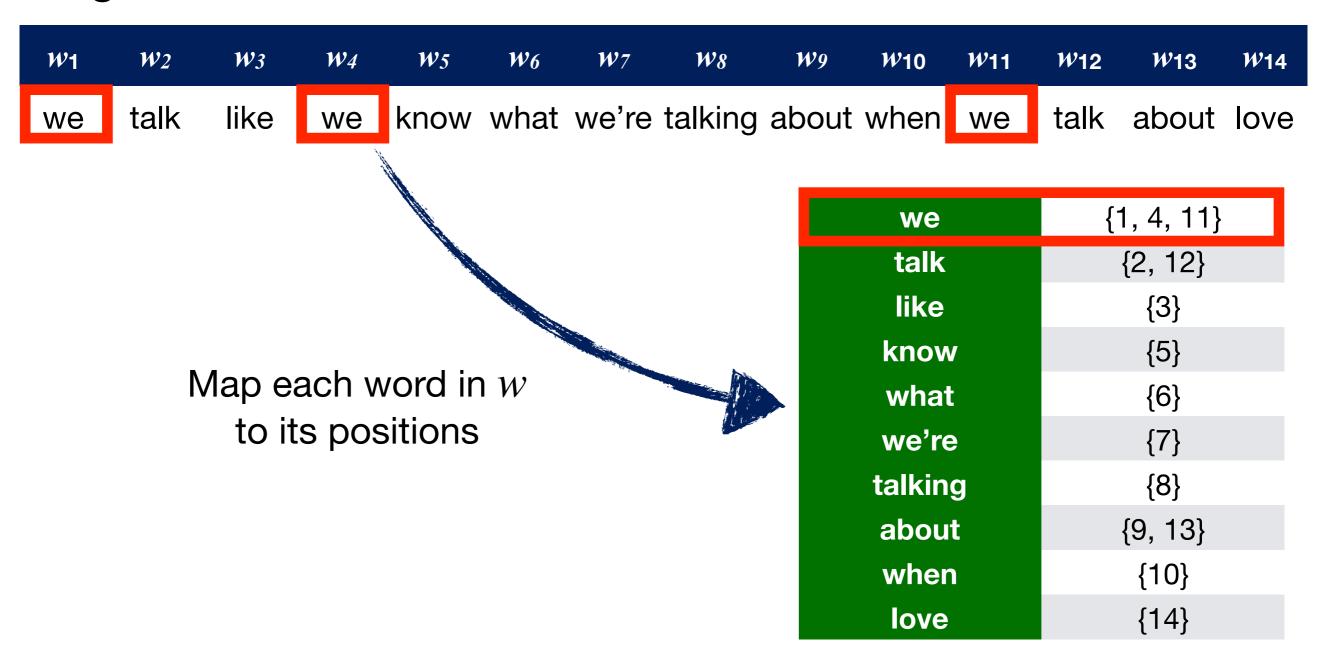


Map each word in *w* to its positions

we	{1, 4, 11}
talk	{2, 12}
like	{3}
know	{5}
what	{6 }
we're	{7}
talking	{8}
about	{9, 13}
when	{10}
love	{14}

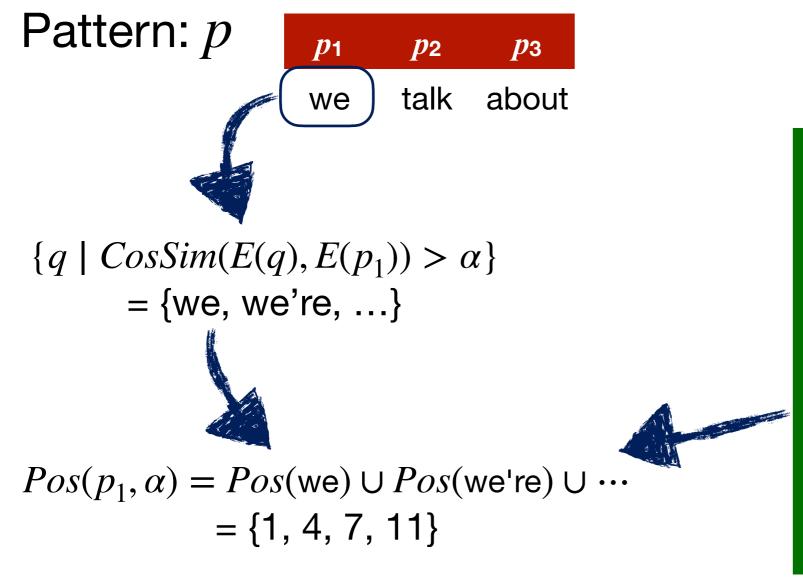
Step 0: Indexing from target

Target w



Step 1: Compute Pointwise Matching Positions

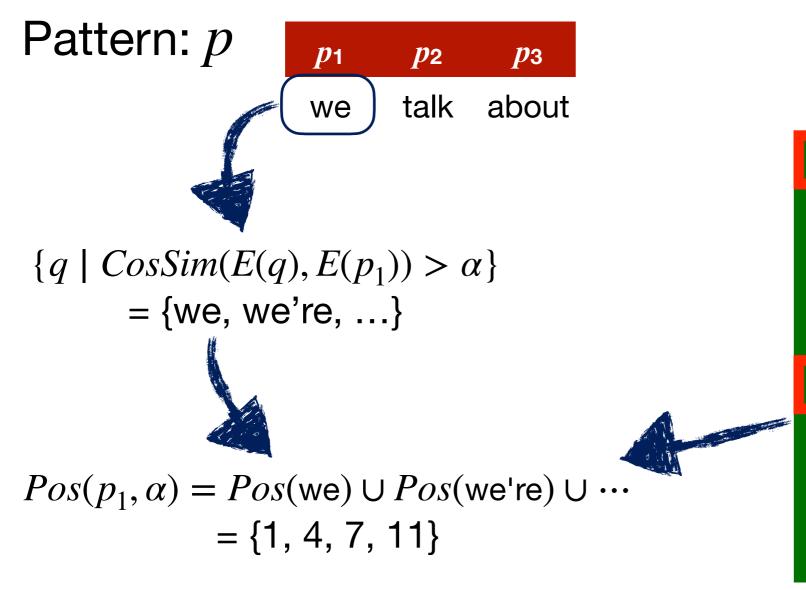
Idea: "Expand" words in pattern and take union



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Step 2: Merge Pointwise Matching Positions by Shift + Intersection

$$Match_{\alpha}(w,p) = \bigcap_{j} \{i - j + 1 \mid i \in Pos(p_{j},\alpha)\}$$

Pattern: *p*



$$Pos(p_1, \alpha) = \{1, 4, 7, 11\}$$

 $Pos(p_2, \alpha) = \{2, 8, 12\}$
 $Pos(p_3, \alpha) = \{9, 13\}$
 $\rightarrow Match_{\alpha}(w, p) = \{7, 11\}$

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Match each pattern word

$$Match_{\alpha}(w,p) = \bigcap_{j} \{i-j+1 \mid i \in Pos(p_{j},\alpha)\}$$

Pattern: *p*

<i>p</i> 1	<i>p</i> ₂	<i>p</i> 3
we	talk	about

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Compensate the offset

$$Match_{\alpha}(w, p) = \bigcap_{j} \{i - j + 1 \mid i \in Pos(p_{j}, \alpha)\}$$

Pattern: *p*

<i>p</i> 1	p ₂	<i>p</i> 3
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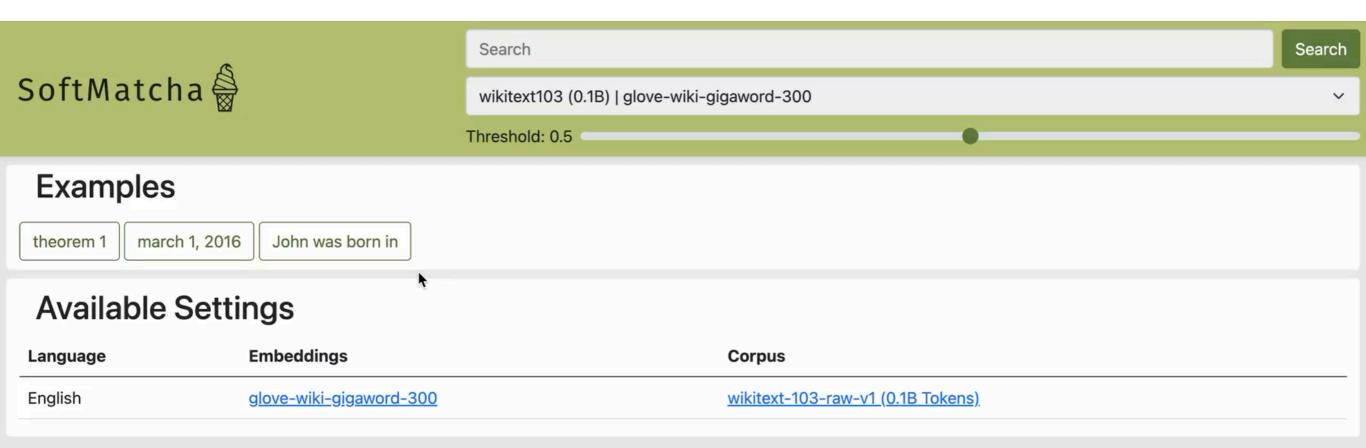
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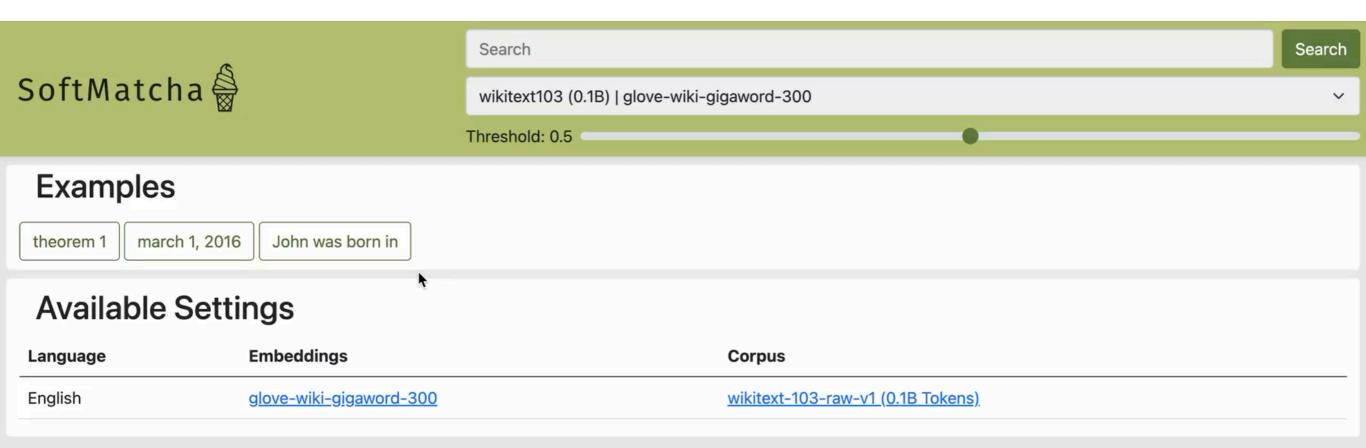


SoftMatcha



- Tool for soft pattern matching
 - Works on laptop w/o GPU
- \$ pip install softmatcha
- Online demo is available
 - Target: text from Wikipedia







Examples

theorem 1

march 1 2016

John was born in

Results

Hits: 7

Search Time: 0.038 sec

Since A-K-L is a straight line, parallel to BD, then rectangle BDLK has twice the area of triangle ABD because they share the base BD and have the same altitude BK, i.e., a line normal to their common base, connecting the parallel lines BD and AL. (lemma 2)

Surface diffusion kinetics can be thought of in terms of adatoms residing at adsorption sites on a 2D lattice, moving between adjacent (nearest-neighbor) adsorption sites by a jumping process. The jump rate is characterized by an attempt frequency and a thermodynamic factor that dictates the probability of an attempt resulting in a successful jump. The attempt frequency v is typically taken to be simply the vibrational frequency of the adatom, while the thermodynamic factor is a Boltzmann factor dependent on temperature and Ediff, the potential energy barrier to diffusion. Equation 1 describes the relationship:

Where v and Ediff are as described above, Γ is the jump or hopping rate, T is temperature, and kB is the Boltzmann constant. Ediff must be smaller than the energy of desorption for diffusion to occur, otherwise desorption processes would dominate. Importantly, equation 1 tells us how very strongly the jump rate varies with temperature. The manner in which diffusion takes place is dependent on the relationship between Ediff and kBT as is given in the thermodynamic factor: when Ediff < kBT the thermodynamic factor approaches unity and Ediff ceases to be a meaningful barrier to diffusion. This case, known as mobile diffusion, is relatively uncommon and has only been observed in a few systems. For the phenomena described throughout this article, it is assumed that Ediff > > kBT and therefore Γ < < v. In the case of Fickian diffusion it is possible to extract both the v and Ediff from an Arrhenius plot of the logarithm of the diffusion coefficient, D, versus 1 / T. For cases where more than one diffusion mechanism is present (see below), there may be more than one Ediff such that the relative distribution between the different processes would change with temperature.

Surface diffusion is a critically important concept in heterogeneous catalysis, as reaction rates are often dictated by the ability of reactants to " find " each other at a catalyst surface. With increased temperature adsorbed molecules, molecular fragments, atoms, and clusters tend to have much greater mobility (see equation 1). However, with increased temperature the lifetime of adsorption decreases as the factor kBT becomes large enough for the adsorbed species to overcome the barrier to desorption, Q (see figure 2). Reaction thermodynamics aside because of the interplay between increased rates of diffusion and decreased lifetime of adsorption, increased temperature may in



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march 1, 2016

Search

wikitext103 (0.1B) | glove-wiki-gigaword-300

Threshold: 0.5

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theorem 1

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march 1, 2016

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Hits: 7743

Search Time: 0.287 sec

In 2015, Fey created and produced the television comedy Unbreakable Kimmy Schmidt with fellow 30 Rock-alumnus Robert Carlock. The series stars Ellie Kemper as the titular character who escapes from a doomsday cult and moves to New York. It also stars Fey 's former co-star Jane Krakowski, as well as Tituss Burgess (who had previously

appeared in four 30 Rock episodes) and Carol Kane . Although it was originally produced for NBC, it was eventually sold to Netflix and immediately renewed for a second season. The show premiered on March 6, 2015 to critical acclaim.

On July 16, 2015, the series was nominated for seven Primetime Emmy Awards, including Outstanding Comedy Series. Fey herself was nominated both as the creator / executive producer of the series and for Outstanding Guest Actress in a Comedy Series for her guest performance as Marcia, a bumbling prosecutor in reference to Marcia Clark .

In 2015, it was announced Fey would be the narrator for the Disney Nature film Monkey Kingdom, which was released in theaters on April 17, 2015. She then re-teamed with Poehler, starring in the 2015 comedy film Sisters as the title characters, and received positive reviews for her role. In 2016, Fey starred in the biographical war comedy-drama

Whiskey Tango Foxtrot, based on the memoir The Taliban Shuffle: Strange Days in Afghanistan and Pakistan, to positive reviews.

The album was completed on November 2013, and a bonus disc was also made for the album, containing the leftover material from the main album as well as songs from Ghost 2, the unreleased compilation of leftover tracks from Ghost. Originally in 2012, Townsend stated that this album will be the sixth and the last album in the Devin Townsend Project series, but he ultimately confirmed that Casualties of Cool is its own project. Townsend also started a crowdfunding campaign through PledgeMusic to support the release of the album. The funding quickly reached its goal, and all additional funds were put directly to Townsend's upcoming projects. Casualties of Cool was released on May 14 , 2014 . The album was re-issued worldwide on January 15 , 2016 containing an additional DVD with live footage from the 2014 concert at the Union Chapel in London



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Case Study: finding harmful phrases

Target: corpus in Wikipedia articles (3.4B words)

Pattern: homemade bombs

	Exact Matching	g SoftMatcha	Dense vector search
Match Examples	homemade bombs	homemade bombshome-made	Article: Survival under atomic attackArticle: Mark 24
	oft" matching but owing the pattern	grenadeshomemademissiles	nuclear bombsArticle: List of common misconceptions

Case Study: finding harmful phrases

Target: corpus in Wikipedia articles (3.4B words)

Pattern: homemade bombs

	Exact Matching	SoftMatcha	Dense vector search
Indexing	685.8 sec	685.8 sec	1036.5 sec
Search	0.005 sec	0.098 sec	0.389 sec
	Slower than exact matching but fast		

Q. Can we use this for monitoring/testing?

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A. Technically Yes. Practically No so far.

Open Problem: Making Spec.

- Making spec. for LLM seems tricky
- Somewhat similar to perception component in automated driving

- The application is too wide
- The expected behavior highly depends on the context
- Prohibiting inappropriate words is possible, but can be done more naively
- Perhaps inferring component-level spec from systemlevel spec?

Conclusions

- We can make pattern matching "soft" w/ a distance
 - Word embedding + cosine similarity
- Indexing-based approach can handle billion-scale corpus
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Any ideas are welcome!